

# Using Abstraction in Multi-Rover Scheduling

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# Motivation

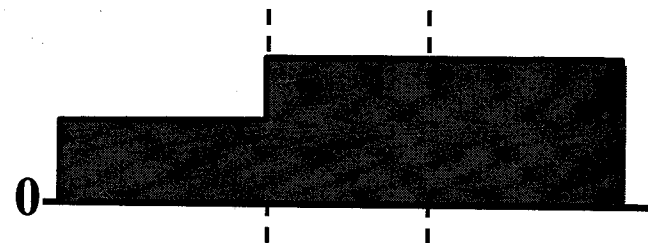
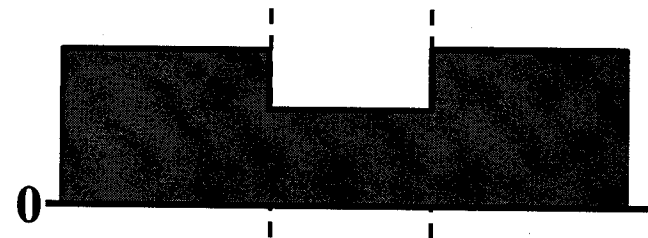
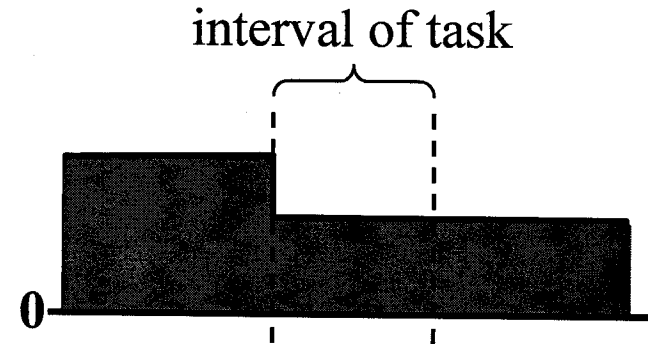
- Current trends within NASA programs point toward a need to coordinate flight projects to:
  - manage shared resources or
  - generate multiple sensor science products.
- Operations staffs must coordinate the schedules of these interacting spacecraft (or instruments).
- Reasoning about schedules at abstract levels offers performance advantages in resolving schedule coordination conflicts.
- Resolving conflicts at abstract levels preserves choices in plan refinement for flexible execution.

# Contributions

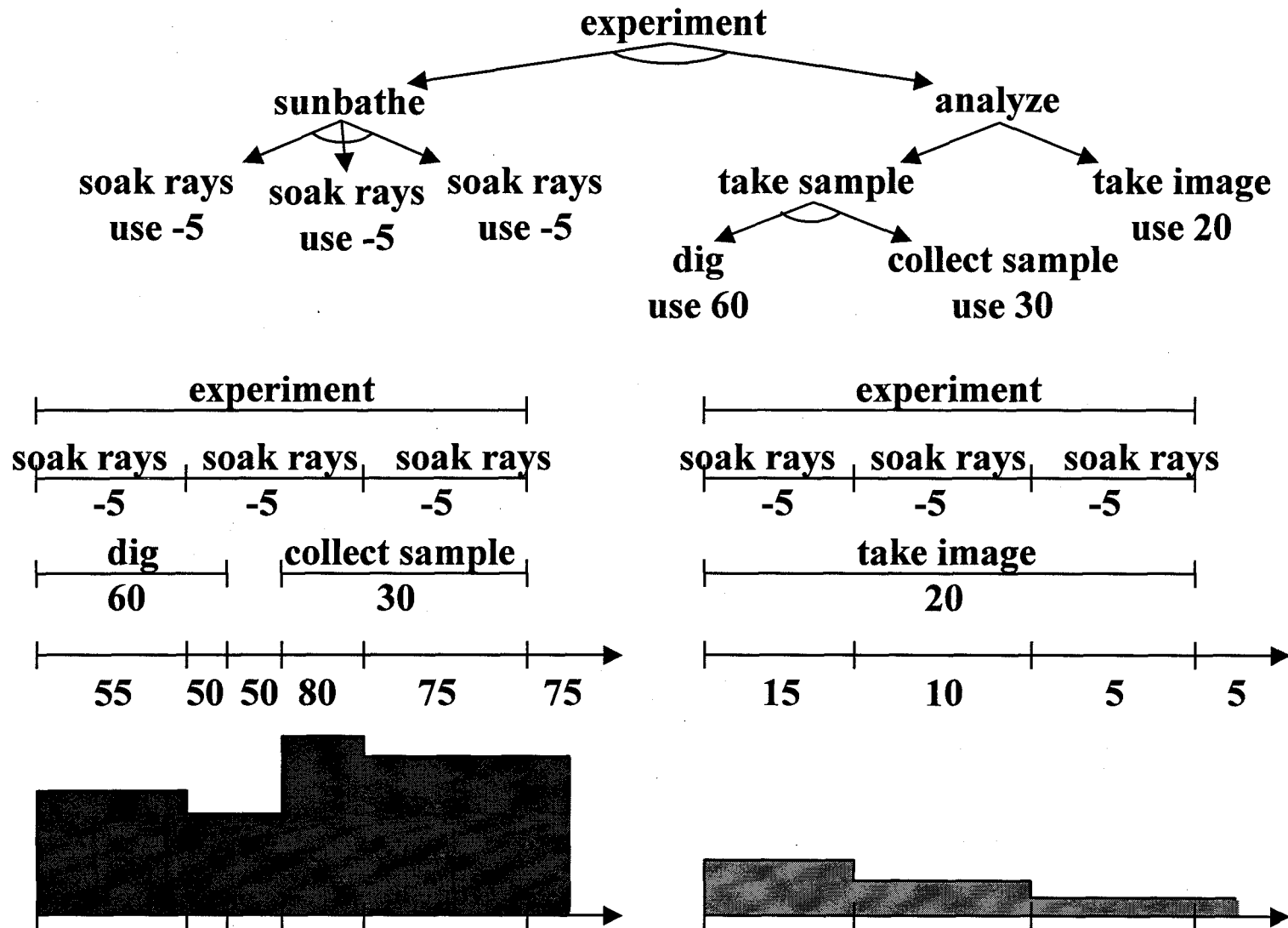
- Algorithm summarizing metric resource usage for abstract activities
- Complexity analysis showing that iterative repair scheduling operations are exponentially cheaper at higher levels of abstraction when summarizing activities results in fewer constraints and temporal constraints
- Experiments in a multi-rover domain that support the analysis
- Comparison of search techniques for directing the refinement of activities in an iterative repair planner that show how summary information can further improve performance in finding solutions

# Resource Usage

- Depletable resource
  - usage carries over after end of task
  - $gas = gas - 5$
- Non-depletable
  - usage is only local
  - zero after end of task
  - $machines = machines - 2$
- Replenishing a resource
  - negative usage
  - $gas = gas + 10$
  - can be depletable or non-depletable



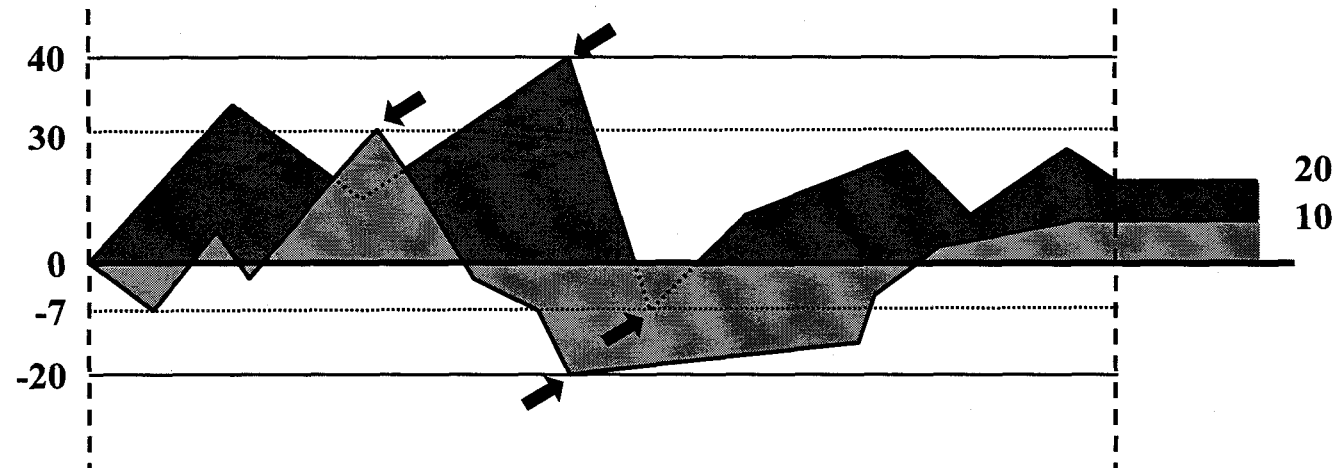
# Summarizing Resource Usage



# Summarizing Resource Usage

*summarized resource usage*  $\equiv$

$\langle \text{local\_min\_range}, \text{local\_max\_range}, \text{persist\_range} \rangle$



$\langle [-7, -20], [30, 40], [10, 20] \rangle$

Captures uncertainty of decomposition choices and  
temporal uncertainty of partially ordered actions

# Resource Summarization Algorithm

- Can be run offline for a domain model
- Run separately for each resource
- Recursive from leaves up hierarchy
- Summarizes parent from summarizations of immediate children
- Considers all legal orderings of children
- Considers all subintervals where upper and lower bounds of children's resource usage may be reached
- Exponential with number of immediate children, so summarization is really constant for one resource and  $O(r)$  for  $r$  resources

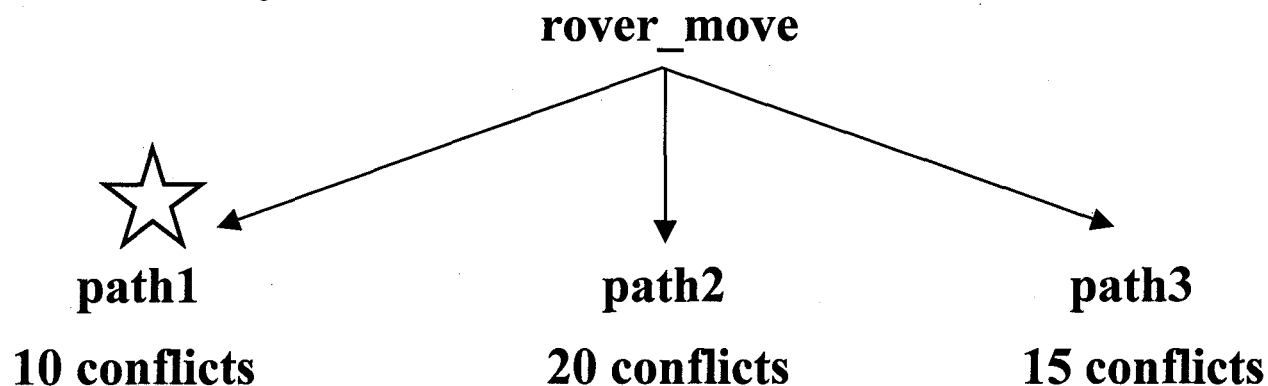
# Decomposition Strategies

- Expand most threats first (EMTF)
  - instead of moving activity to resolve conflict, decompose with some probability (decomposition rate)
  - expands activities involved in greater numbers of conflicts (threats)
- Level expansion
  - repair conflicts at current level of abstraction until conflicts cannot be further resolved
  - then decompose all activities to next level and begin repairing again
- Relative performance of two techniques depends decomposition rate selected for EMTF



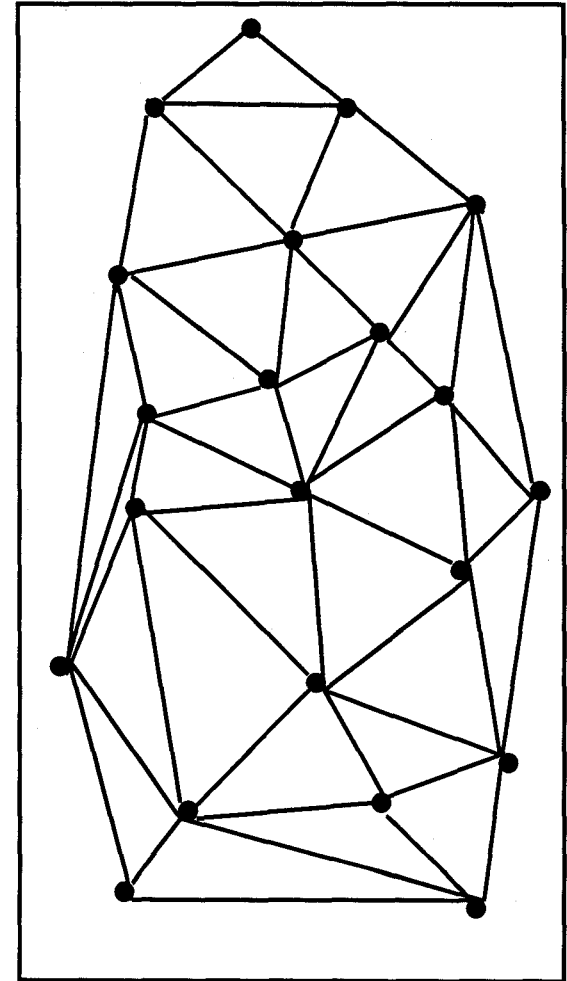
# Decomposition Strategies

- FTF (fewest-threats-first) heuristic tests each decomposition choice and picks those with fewer conflicts with greater probability.



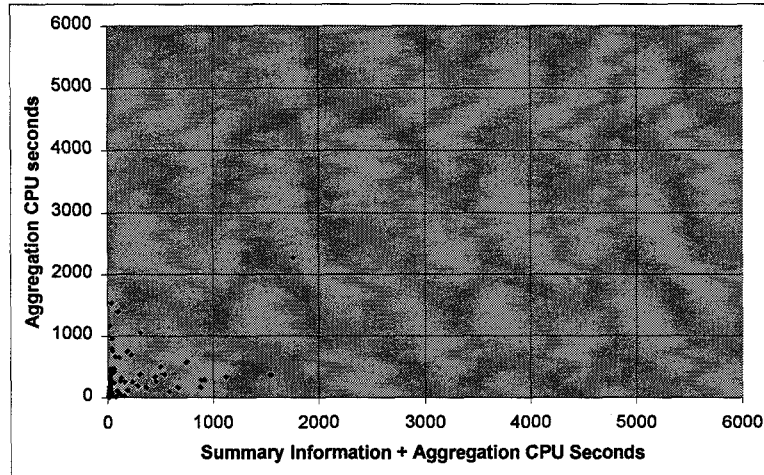
# Multi-Rover Domain

- 2 to 5 rovers
- Triangulated field of 9 to 105 waypoints
- 6 to 30 science locations assigned according to a multiple travelling salesman algorithm
- Rovers' plans contain 3 shortest path choices to reach next science location
- Paths between waypoints have capacities for a certain number of rovers
- Rovers cannot be at same location at the same time
- Rovers cannot cross a path in opposite directions at the same time
- Rovers communicate with the lander over a **shared** channel for telemetry--different paths require more bandwidth than others

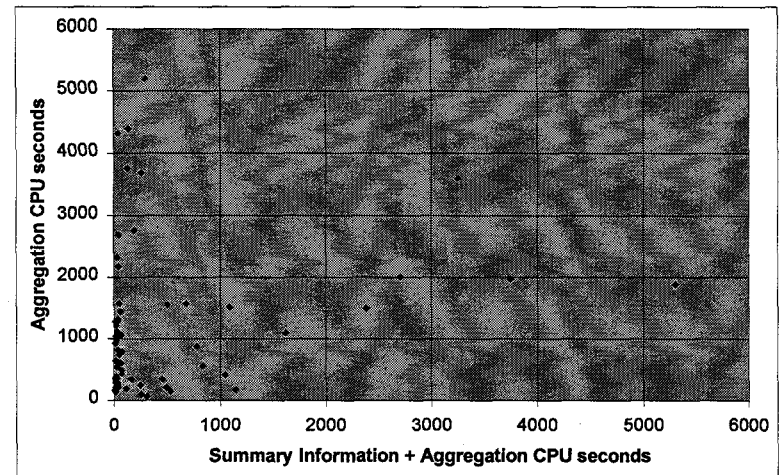


# Experiments in ASPEN for a Multi-Rover Domain

- Performance improves greatly when activities share a common resource.

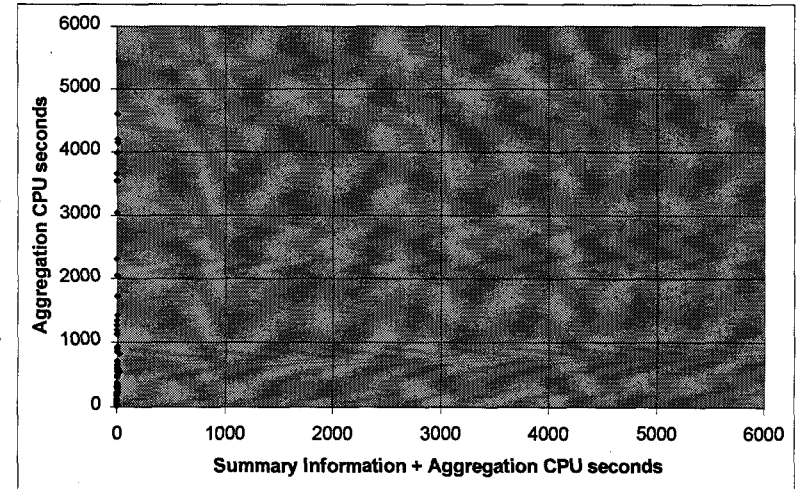
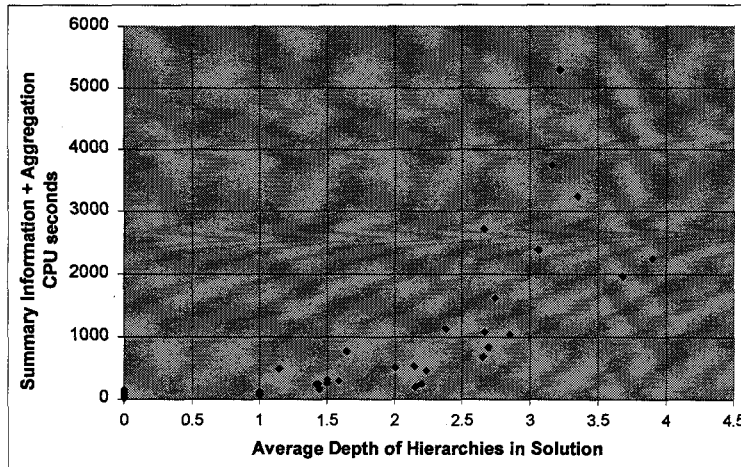


**Rarely shared resources (only path variables)**



**Mix of rarely shared (paths) and often shared (channel) resources**

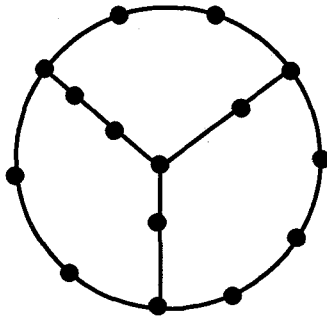
- CPU time required increases dramatically for solutions found at increasing depth levels.



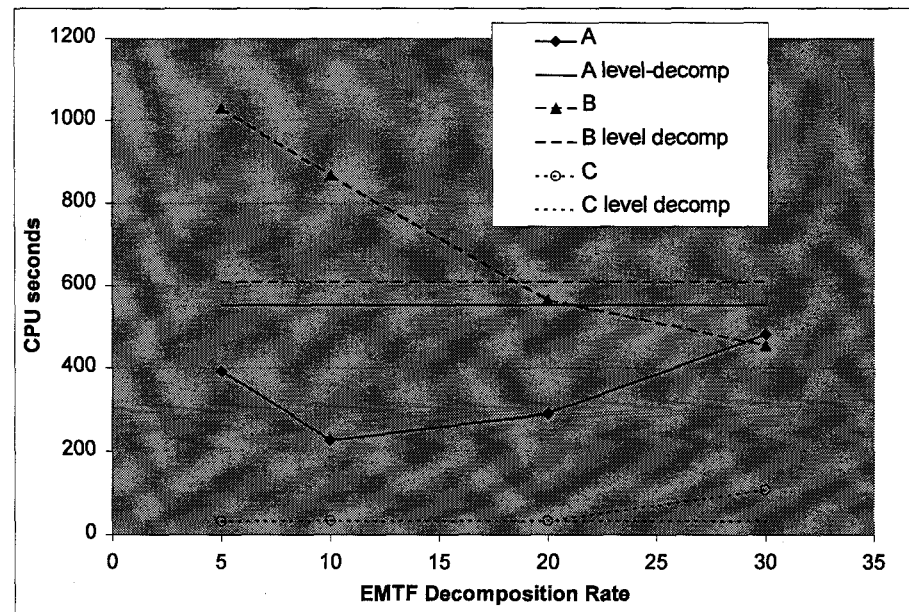
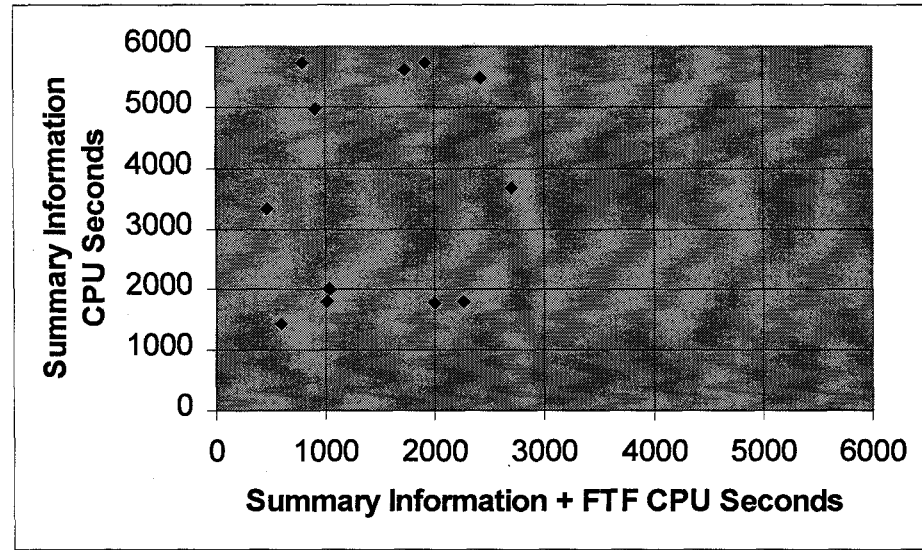
**Often shared (channel) resource only**

# Experiments in ASPEN for a Multi-Rover Domain

- Picking branches that result in fewer conflicts (FTF) greatly improves performance.

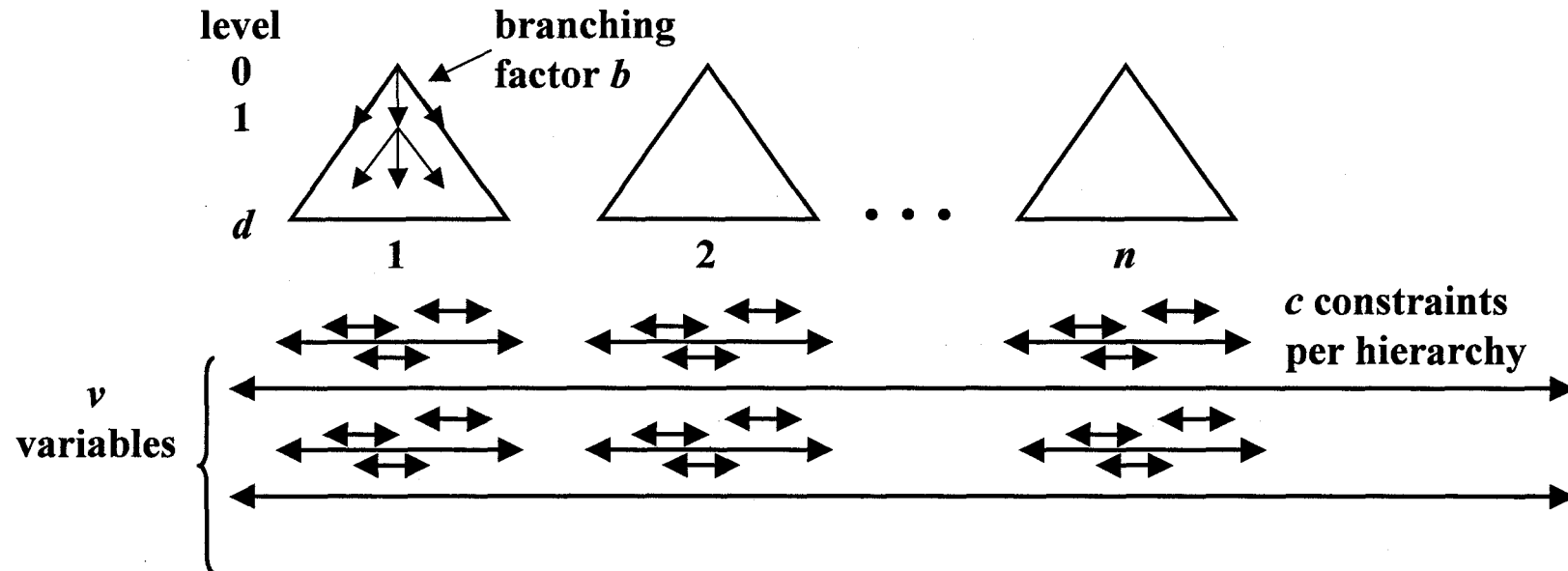


- Expanding activities involved in greater numbers of conflicts is better than level-by-level expansion when choosing a proper rate of decomposition



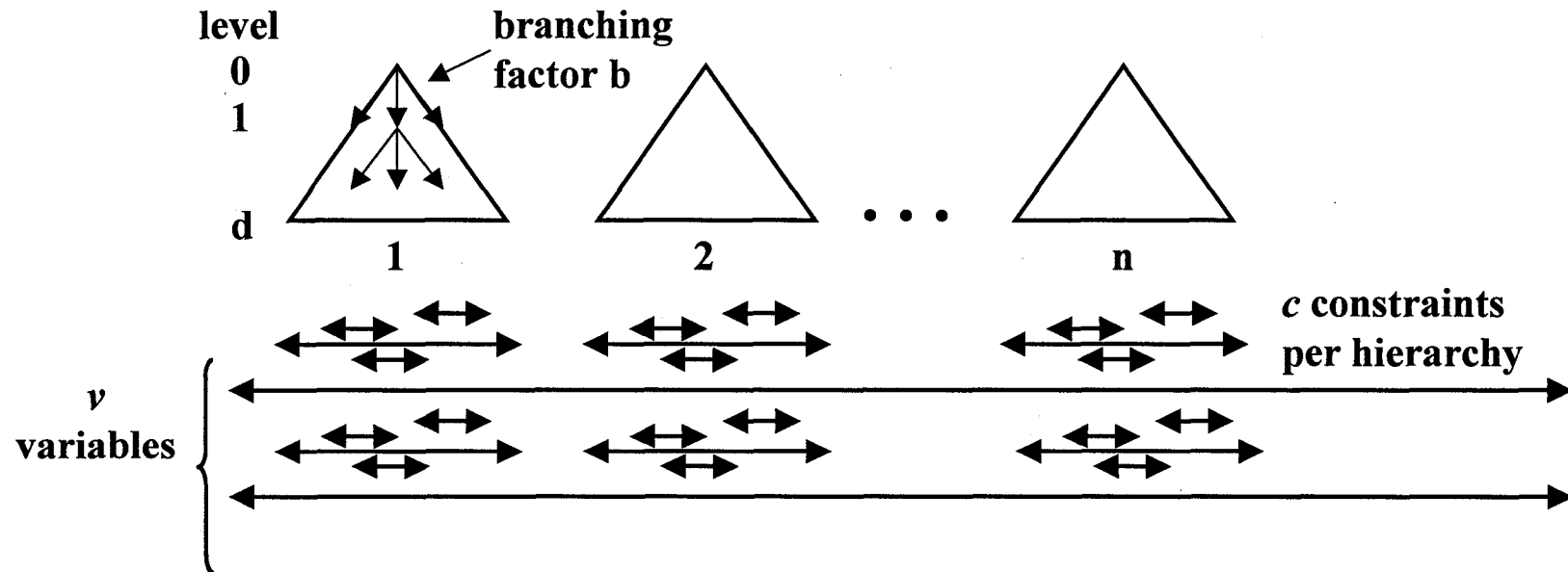
# Complexity Analysis

- Iterative repair planners (such as ASPEN) heuristically pick conflicts and resolve them by moving activities and choosing alternative decompositions of abstract activities.



- Moving an activity hierarchy to resolve a conflict is  $O(vnc^2)$  for  $v$  state or resource variables,  $n$  hierarchies in the schedule, and  $c$  constraints in hierarchy per variable.
- Summarization can collapse the constraints per variable making  $c$  smaller.
- In the worst case, where no constraints are collapsed because they are over different variables, the complexity of moving and activity hierarchies at different levels of expansion is the same.

# Complexity Analysis



- In the other extreme, where constraints are always collapsed when made for the same variable, the number of constraints  $c$  is the same as the number of activities and grows  $b^i$  for  $b$  children per activity and depth level  $i$ . Thus, the complexity of scheduling operations grows  $O(vnb^{2i})$ .
- Along another dimension, the number of temporal constraints that can cause conflicts during scheduling grows exponentially ( $O(b^i)$ ) with the number of activities as hierarchies are expanded.
- In addition, by using summary information to prune decomposition choices with greater numbers of conflicts, exponential computation is avoided.
- **Thus, reasoning at abstract levels can resolve conflicts exponentially faster.**